

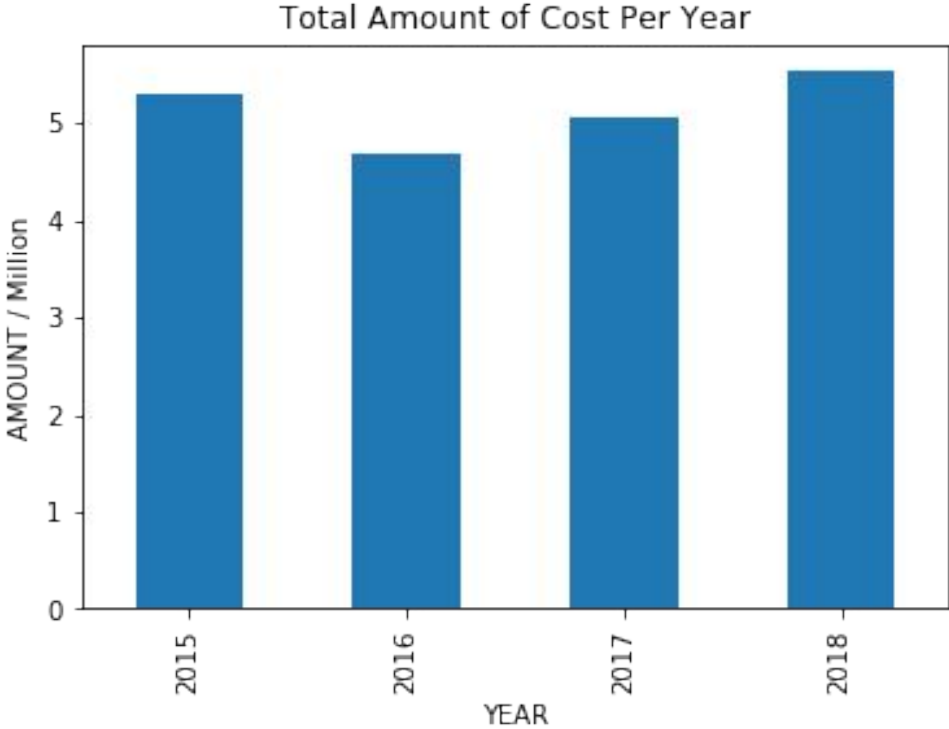
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# Relationship Between Spending and Weather in Madison

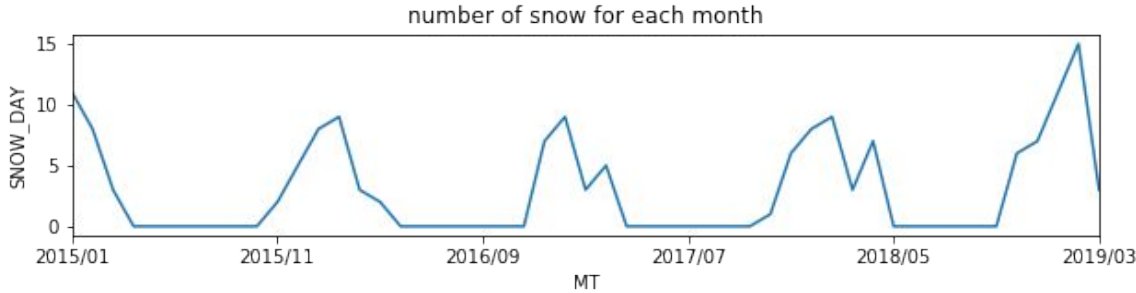
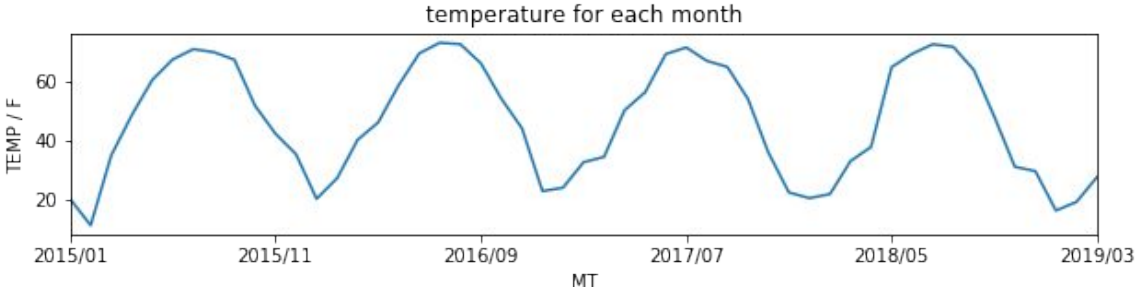
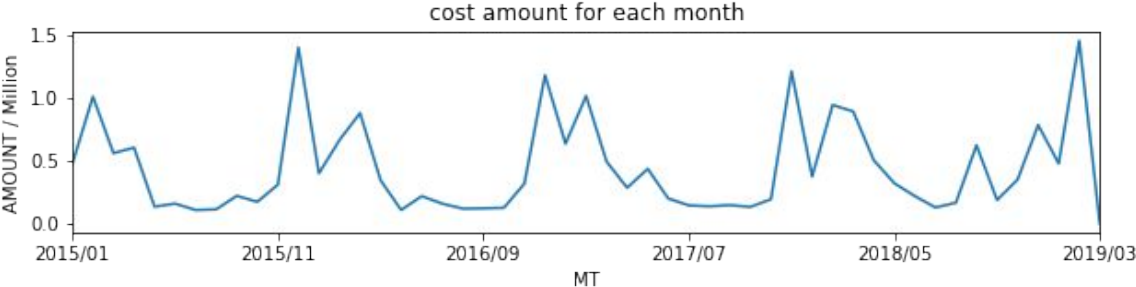


Swaraj Rao  
Whitney Long

# Total Expense in Different Years

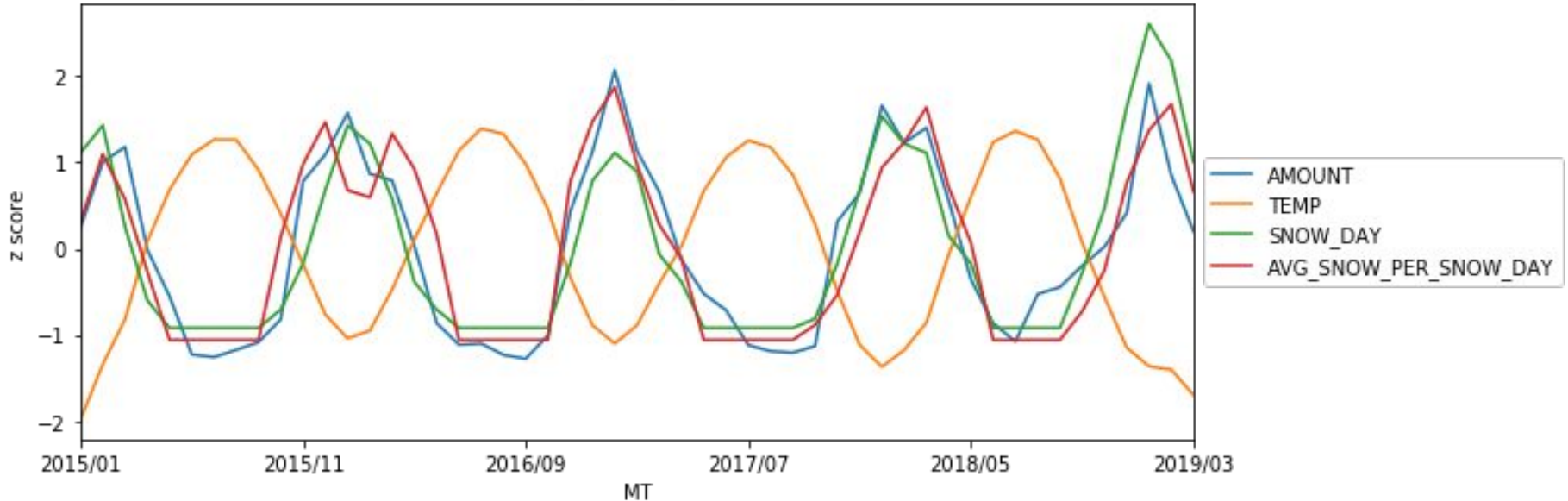


# Overview of historical cost, temperature, and snow



# Data Visualization of Four Examined Variables

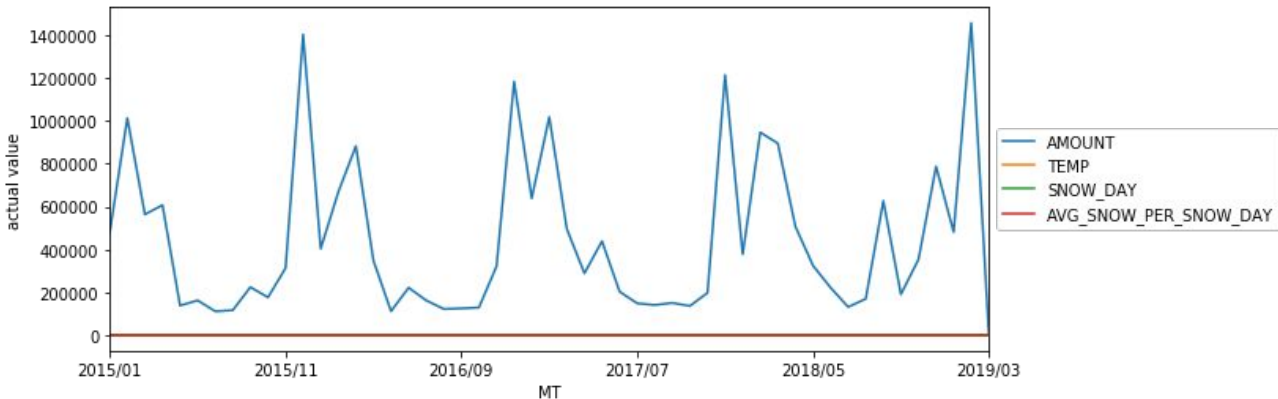
z score of moving average time series data



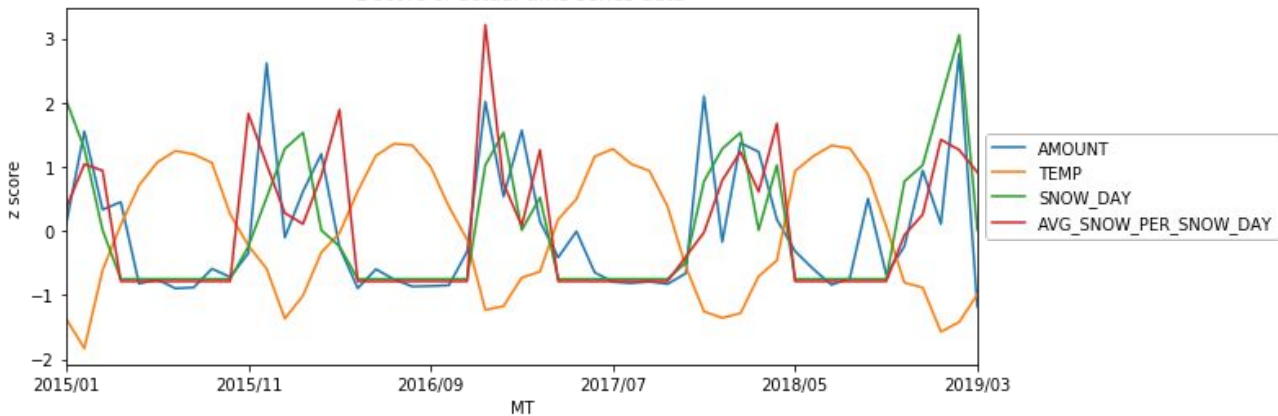
- Instead of using the actual value for each variable, z score, which is computed by minus the mean and divided by standard deviation, is used so that the values are in the same scale.
- Considering the possibility of prepaid and postpaid payments, the real cost amount of one month is estimated by averaging the recorded amount of two adjacent months and itself.

# Why Z-score? Why Moving-average?

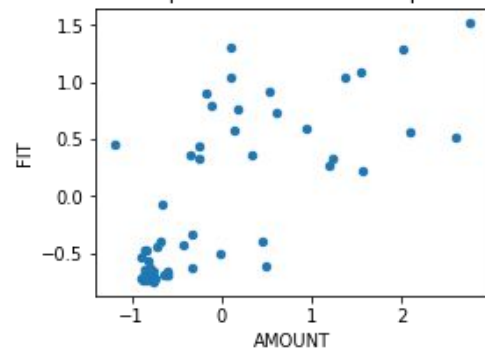
actual value of actual time series data



z score of actual time series data

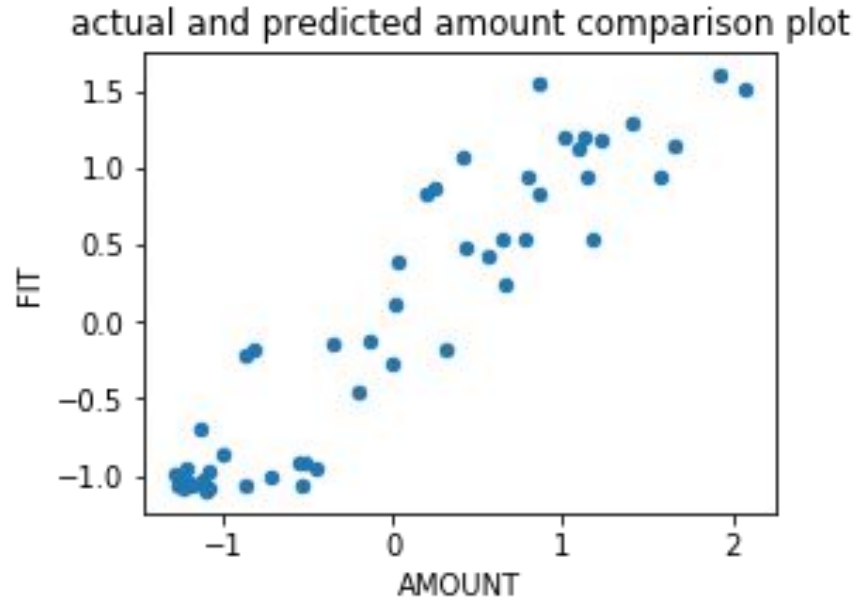


actual and predicted amount comparison plot



Standard Deviation of the difference between actual z score and predicted z score is 0.7097  
Regression without moving average

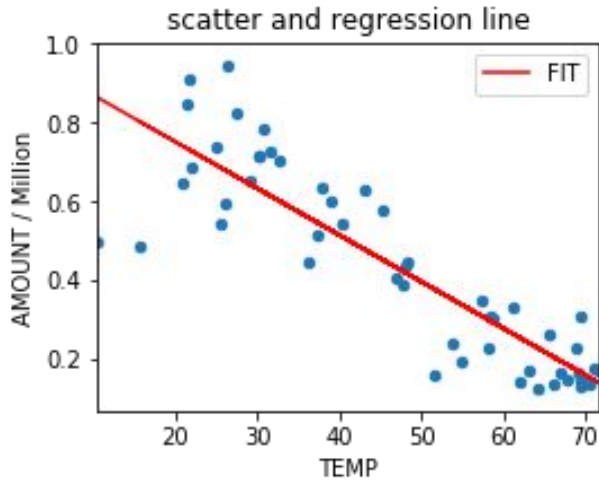
# Linear Regression of Four Variables



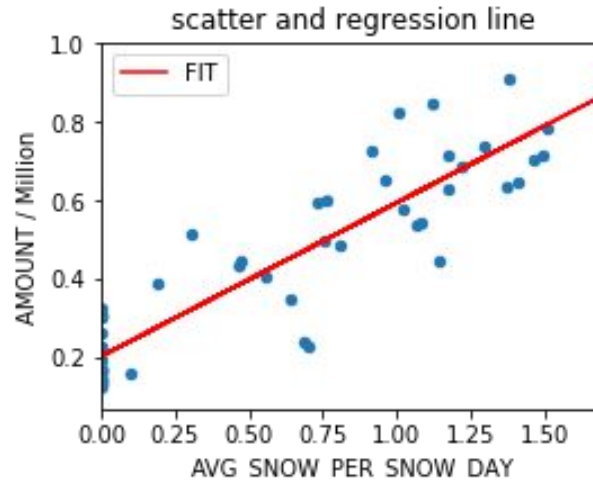
$$\text{AMOUNT} = -0.2483 * \text{TEMP} + 0.2127 * \text{SNOW\_DAY} + 0.5186 * \text{AVG\_SNOW\_PER\_SNOW\_DAY}$$
  
Standard Deviation of the difference between actual z score and predicted z score is 0.3582

## Linear Regression of Each Variable:

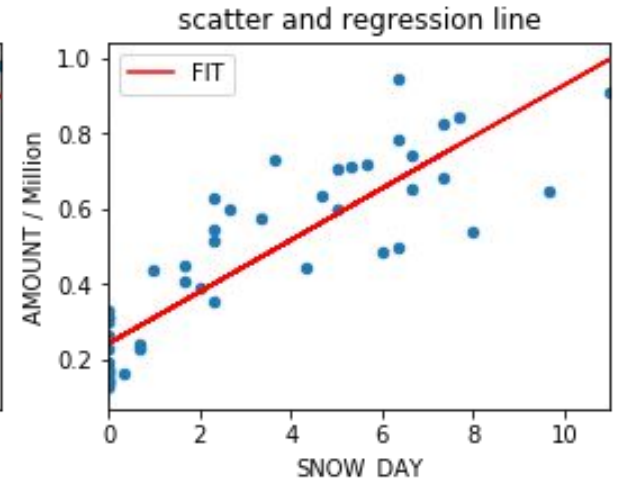
### Temperature, Average Snow Per Snow Day, and the Total Number of Snow Day



Std Err: 0.1193



Std Err: 0.1054



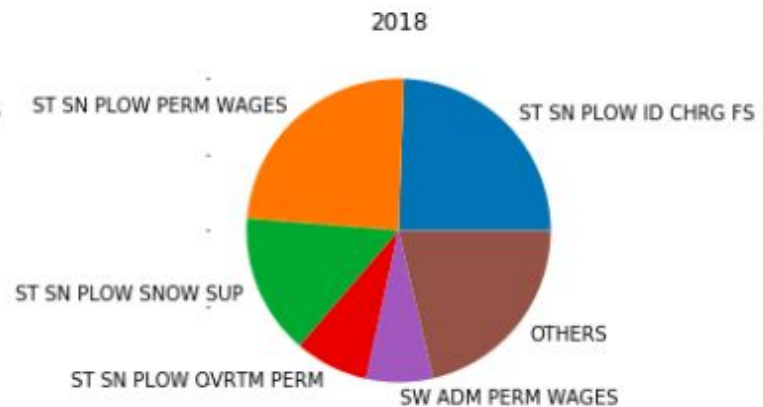
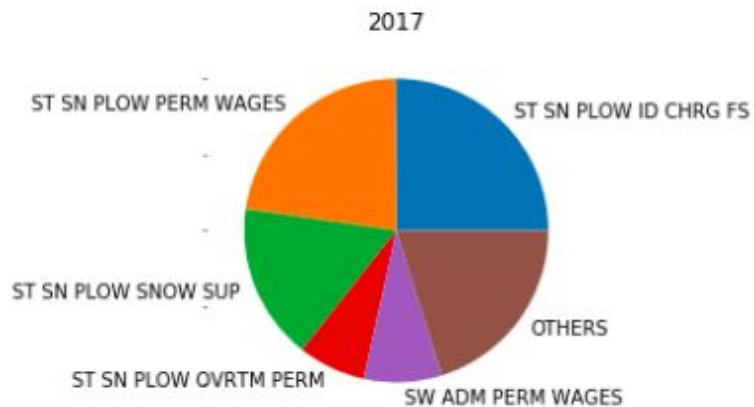
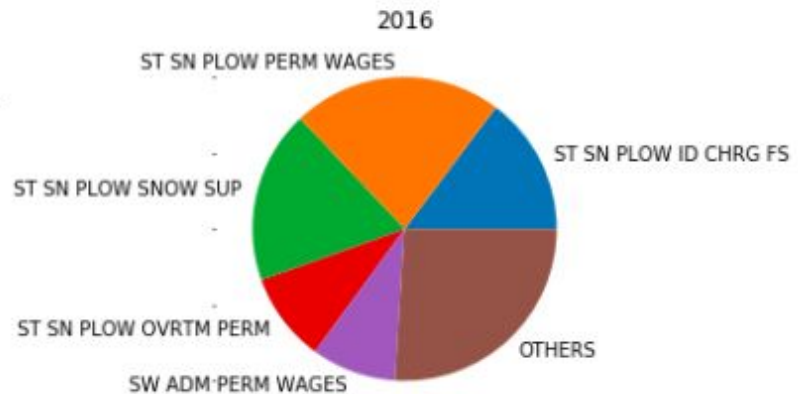
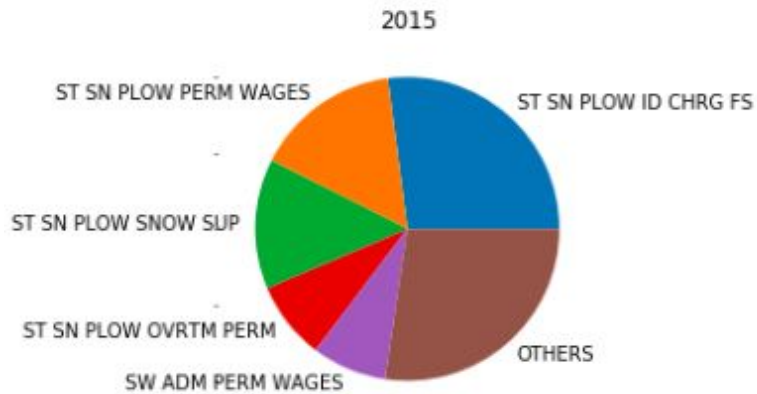
Std Err: 0.1186

$$\text{AMOUNT} = -0.0118 * \text{TEMP} + 0.9868$$

$$\text{AMOUNT} = 0.3910 * \text{AVG\_SNOW\_PER\_SNOW\_DAY} + 0.2032$$

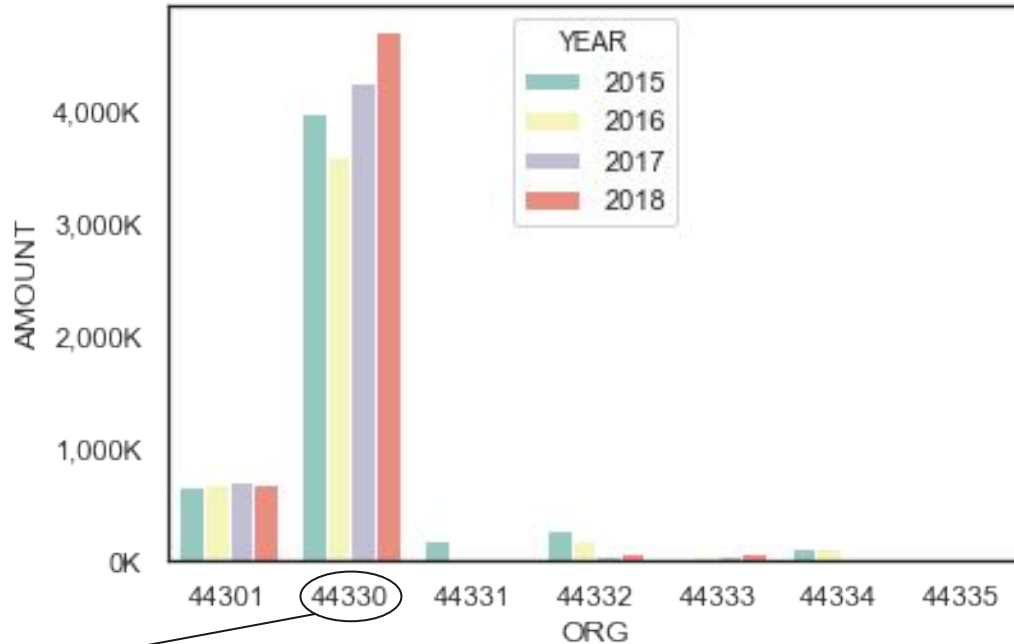
$$\text{AMOUNT} = 0.0689 * \text{SNOW\_DAY} + 0.2407$$

# Proportion of Cost in Different Categories



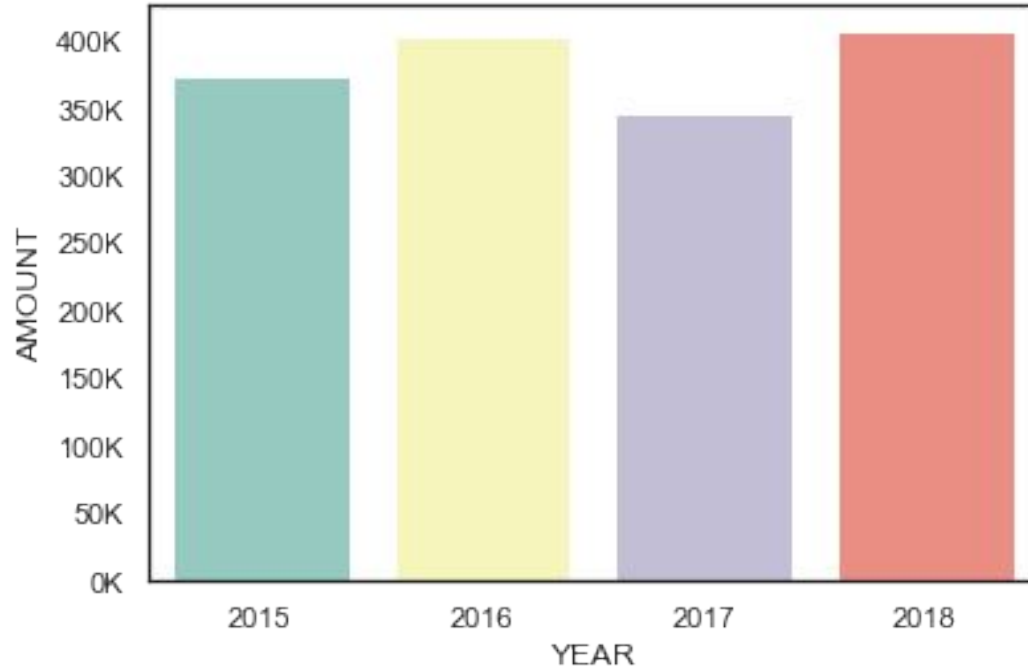


# City spending data by org over that timespan



Snow Plowing organization

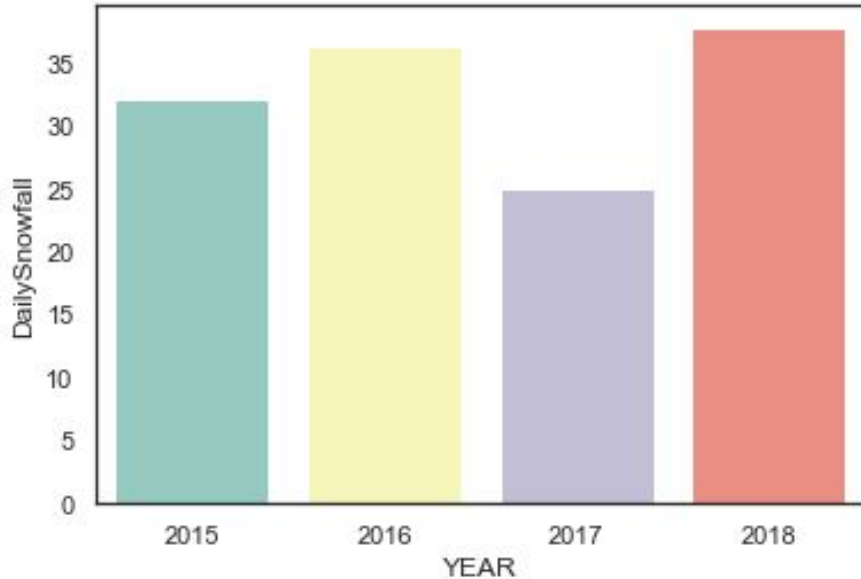
# Snow plowing overtime pay over the years



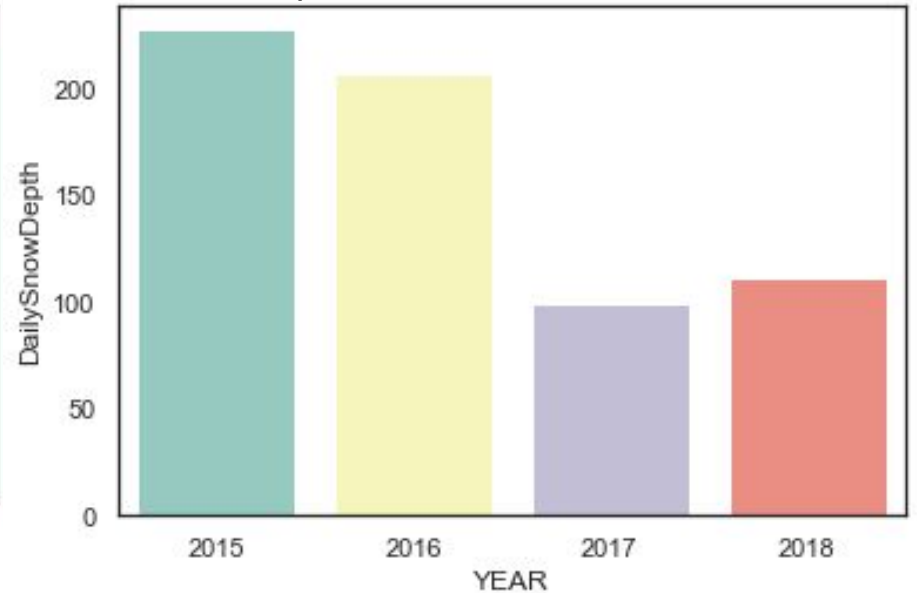
# Cumulative daily snowfall and snow depth



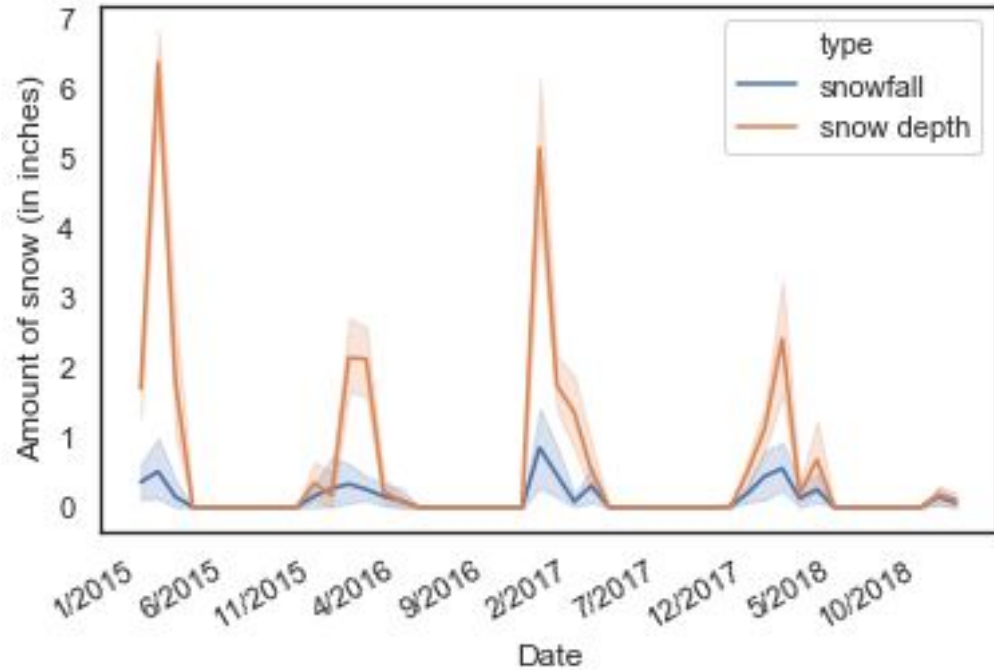
## Snowfall



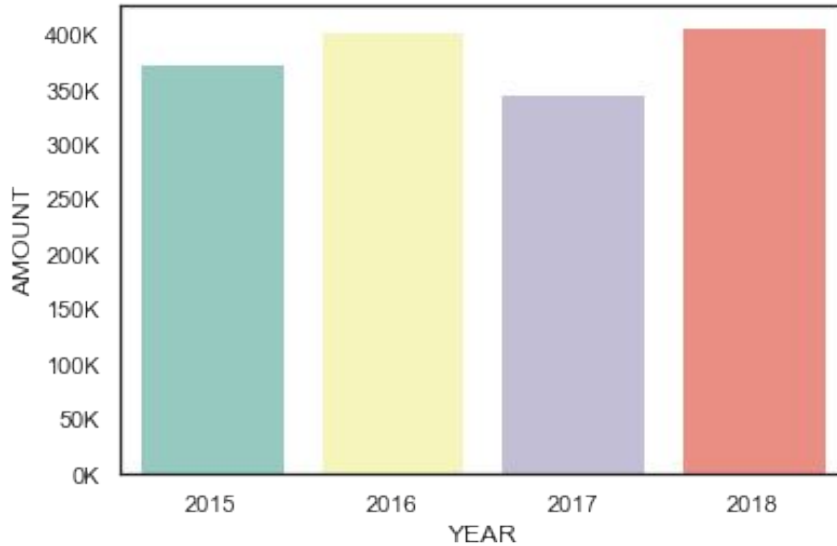
## Snow depth



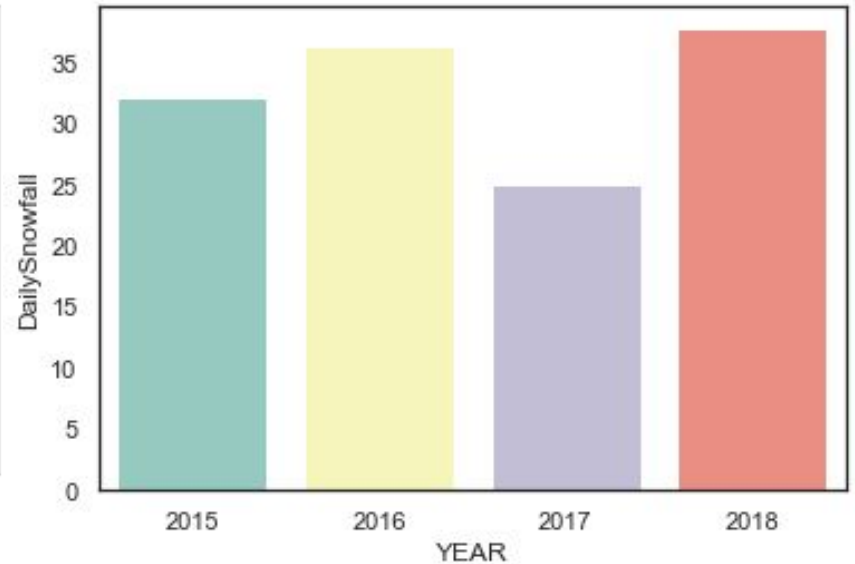
# Comparison of snowfall and snow depth



# Similarities to daily snowfall over the years

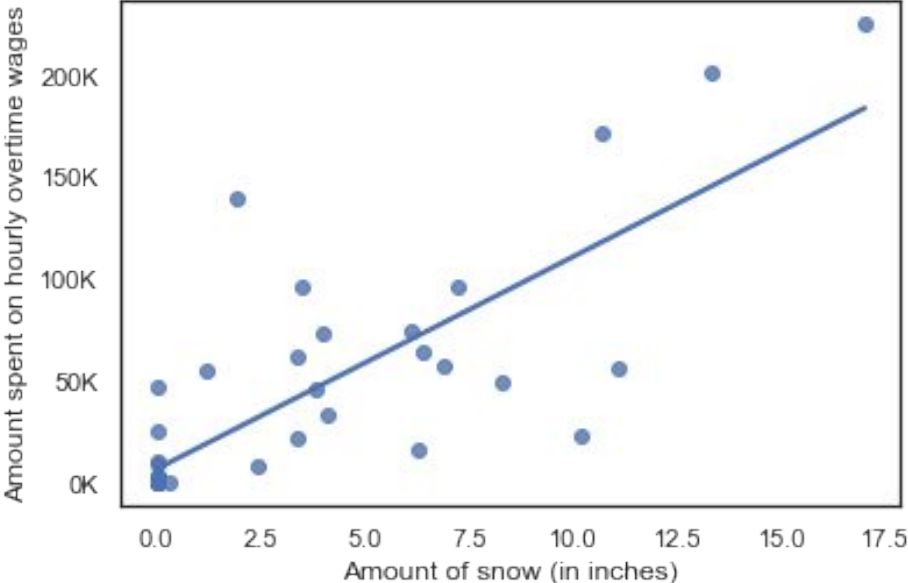


Yearly spending on overtime wages



Yearly cumulative snowfall

# Regression model between monthly spending and snowfall



## Simple linear regression model to predict overtime hourly wages from predicted snowfall

Sum of X = 131.5 Mean X = 2.7396 (where X = monthly snowfall)

Sum of Y = 1702749.35 Mean Y = 35473.9448 (where Y = monthly spending on overtime wages)

Sum of squares (SSX) = 827.0948

Sum of products (SP) = 8607676.0319

Regression Equation =  $\hat{y} = bX + a$

$b = SP/SSX = 8607676.03/827.09 = 10407.12155$

$a = MY - bMX = 35473.94 - (10407.12 \cdot 2.74) = 6962.76804$

$\hat{y} = 10407.12155X + 6962.76804$

# Correlation coefficient of the model

$$r = \frac{1}{n-1} \left( \frac{\sum_x \sum_y (x - \bar{x})(y - \bar{y})}{s_x s_y} \right)$$

WS:

X = monthly cumulative snowfall

Y = monthly cumulative spending on overtime wages

Using this equation our  $r = 0.8071$

$0.7 < |r| \leq 1$  represents a strong correlation between variables





## Predicted spending on overtime wages vs actual spending

	Predicted	Actual	Error
2019	453106.07	347048.18	30%

Using snowfall and spending data from January and February 2019.

# Future

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- At the end of the year, check if regression model has a lower error % when predicting spending on overtime wages
- Possibly use more objects in analysis
  - Snow supplies object
  - Snow plowing object
- Include more variables in regression analysis to decrease standard deviation and find more accurate models



**Questions?**